

**TURKISH
AVIATION
ACADEMY**



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Network Schedule Optimization Extensions

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Network, Fleet and Schedule
Strategic Planning
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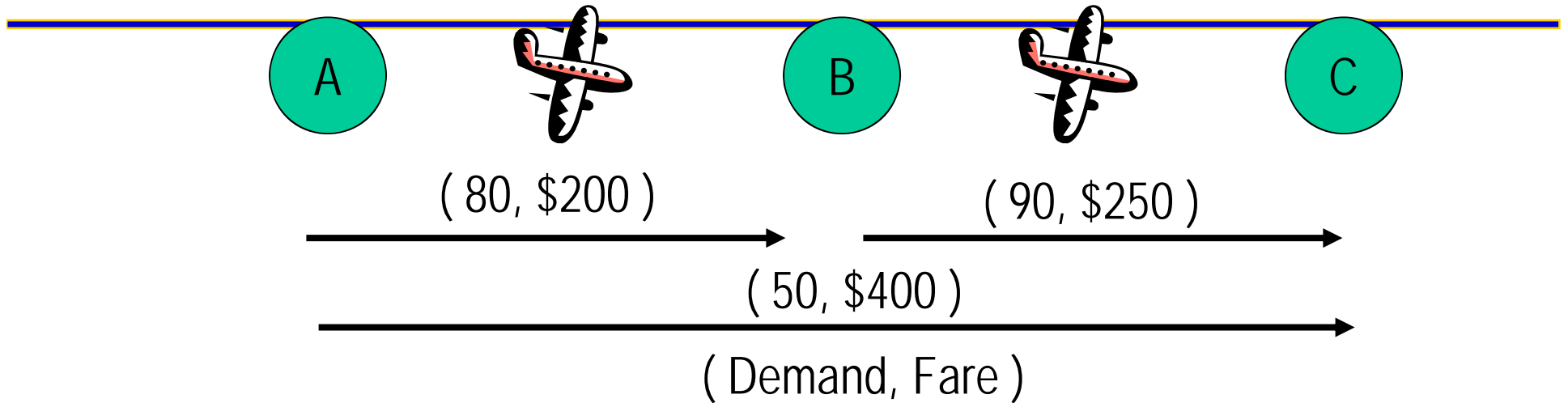
Lecture Outline

- **Itinerary-based Network Fleet Assignment**
 - Network Effects on Evaluating Spill
 - IFAM Definition and Formulation
 - Opportunities for Further Model Improvement
- **Dynamic Fleet Assignment**
 - Demand Driven Dispatch
 - Requirements and Implementation Issues
- **Crew Scheduling Optimization**
 - Definitions and Constraints
 - Crew Pairing Problem

Leg-Based Fleet Assignment Optimization

- **The fleet assignment models examined thus far have assumed independent demand and spill on each leg**
 - In essence, all demand on each leg assumed to be local
 - Changing capacity assumed to affect only demand on that leg, and revenue impact based on fares paid by local demand
 - Certainly not true in a large connecting hub network
- **Several network optimization models were presented, but leg independence was still assumed**
 - “Network” fleet assignment optimization referred to ensuring a balance of aircraft types and feasible rotations of aircraft

Fleet Assignment: Network Effects



Fleet Type	Capacity	Spill Cost
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i	80	?
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ii	100	?
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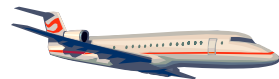
iii	120	?
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iv	150	\$0
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Leg Interdependence

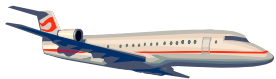
Network Effects

Calculation of Network Spill



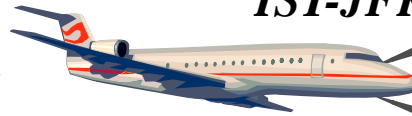
DEL-IST

*30 Connecting Pax
in transit to JFK*



DXB-IST

*25 Connecting Pax
in transit to JFK*



IST-JFK

Capacity: 200

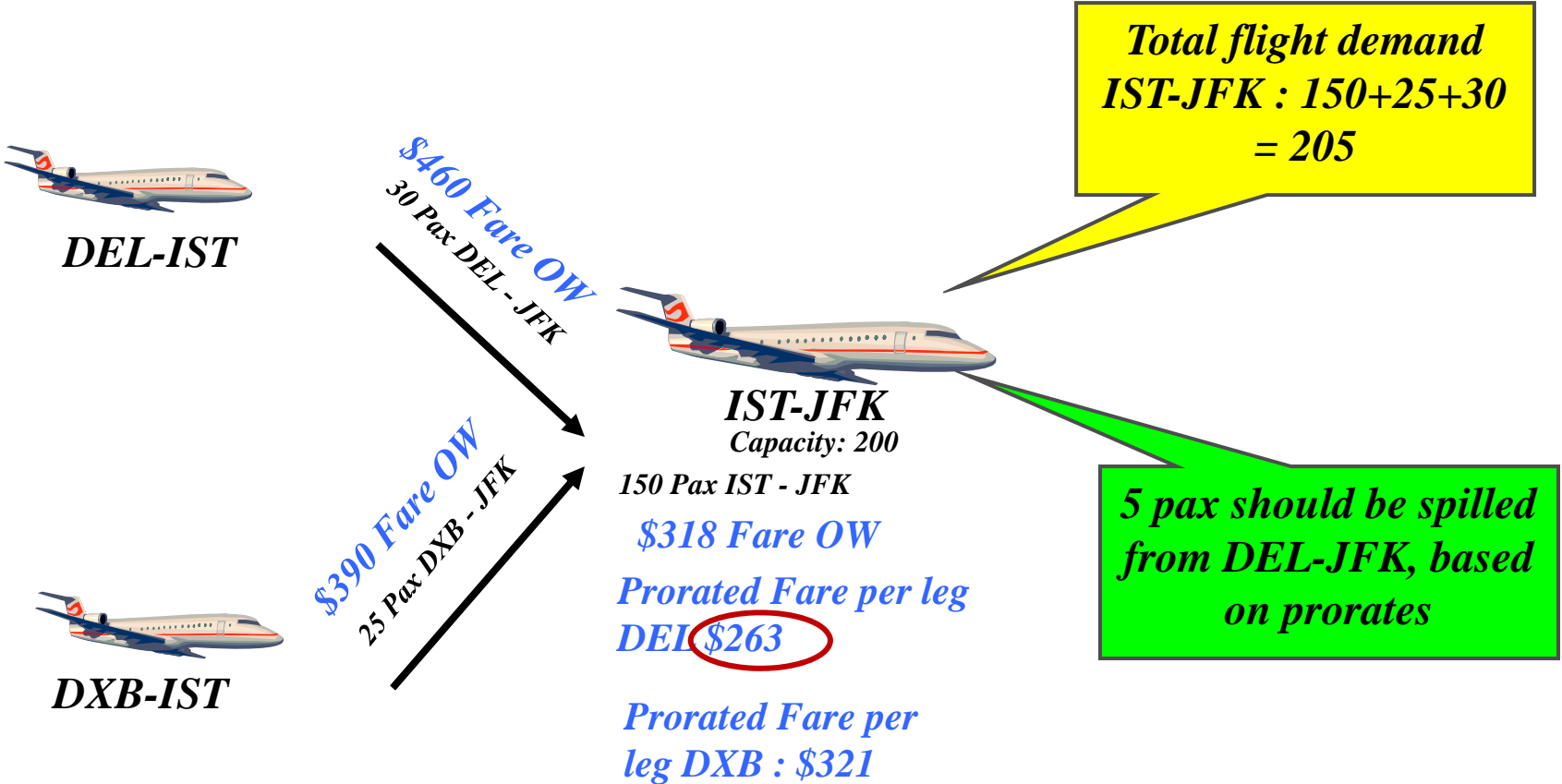
*150 Local Pax travelling
from IST to JFK*

*Total flight demand
IST-JFK : $150+25+30$
= 205*

*Spill
IST-JFK:
 $205-200 = 5$ pax*

Which 5 passengers should be spilled on the IST-JFK flight leg?

Prorated Calculation of Network Spill

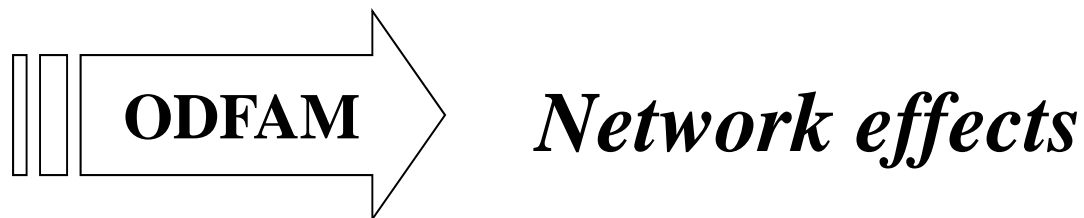


Itinerary-based Fleet Assignment Definition

- **Given**

- a fixed schedule,
- number of available aircraft of different types,
- unconstrained passenger demands by itinerary, and
- recapture rates,

Find maximum contribution



Itinerary-Based FAM (IFAM)

Fleet Assignment

Consistent Spill + Recapture

$$t_p^r \geq 0 \quad f_{k,i} \in \{0,1\} \quad y_{k,o,t} \geq 0$$

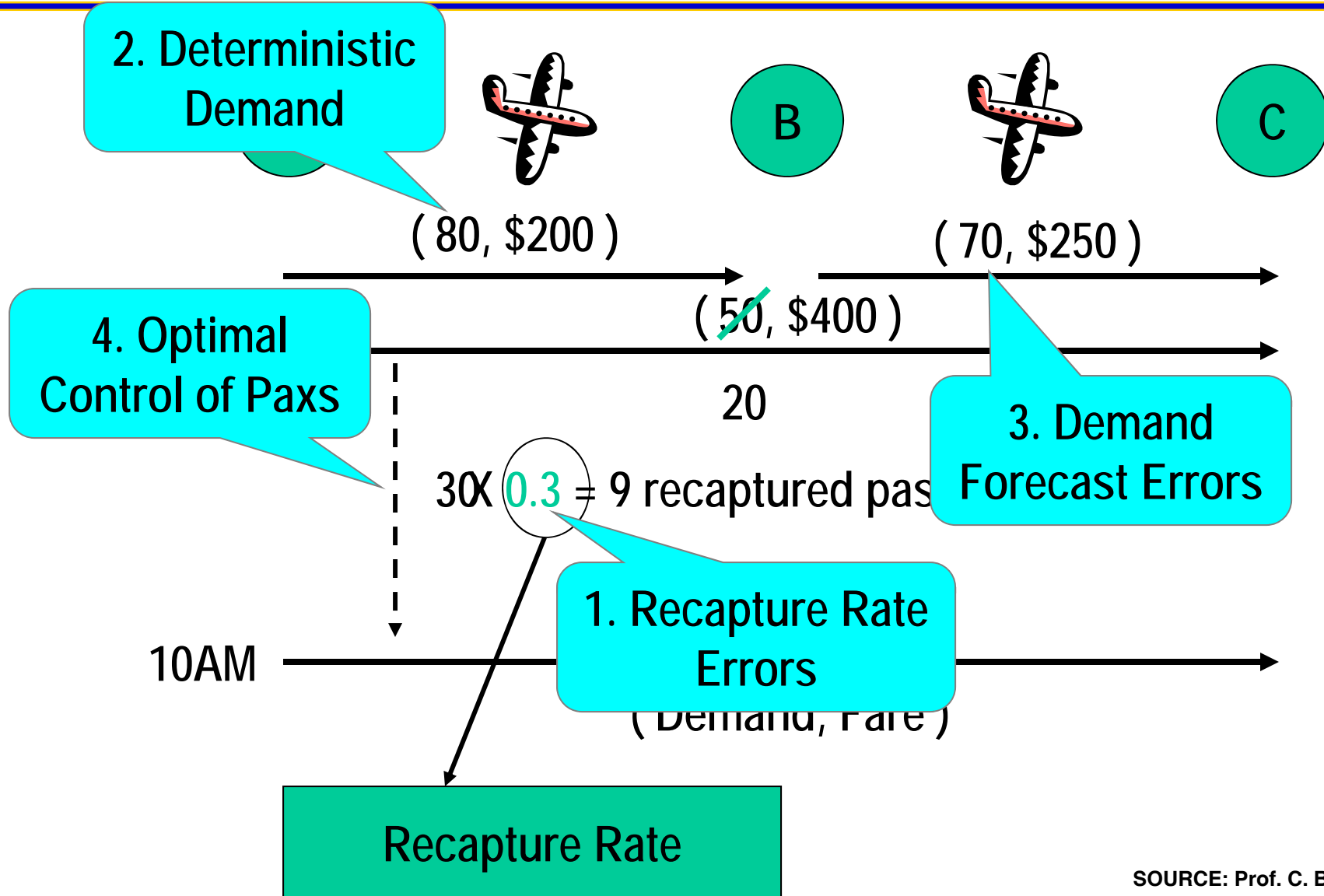
SOURCE: Prof. C. Barnhart

Kniker (1998)

Moving from FAM to IFAM: Challenges

- **IFAM, unlike FAM, has:**
 - Extensive data requirements
 - Itinerary-specific demands
 - Recapture rates
 - Immense model size
 - One decision variable for every pair of itineraries for which spill can occur
 - One constraint for each itinerary
 - Tractability issues associated with model
 - Constraints linking supply (provision of seat capacity) with demand for seats

Opportunities for Improvement: FAM



SOURCE: Prof. C. Barnhart

Dynamic Fleet Assignment

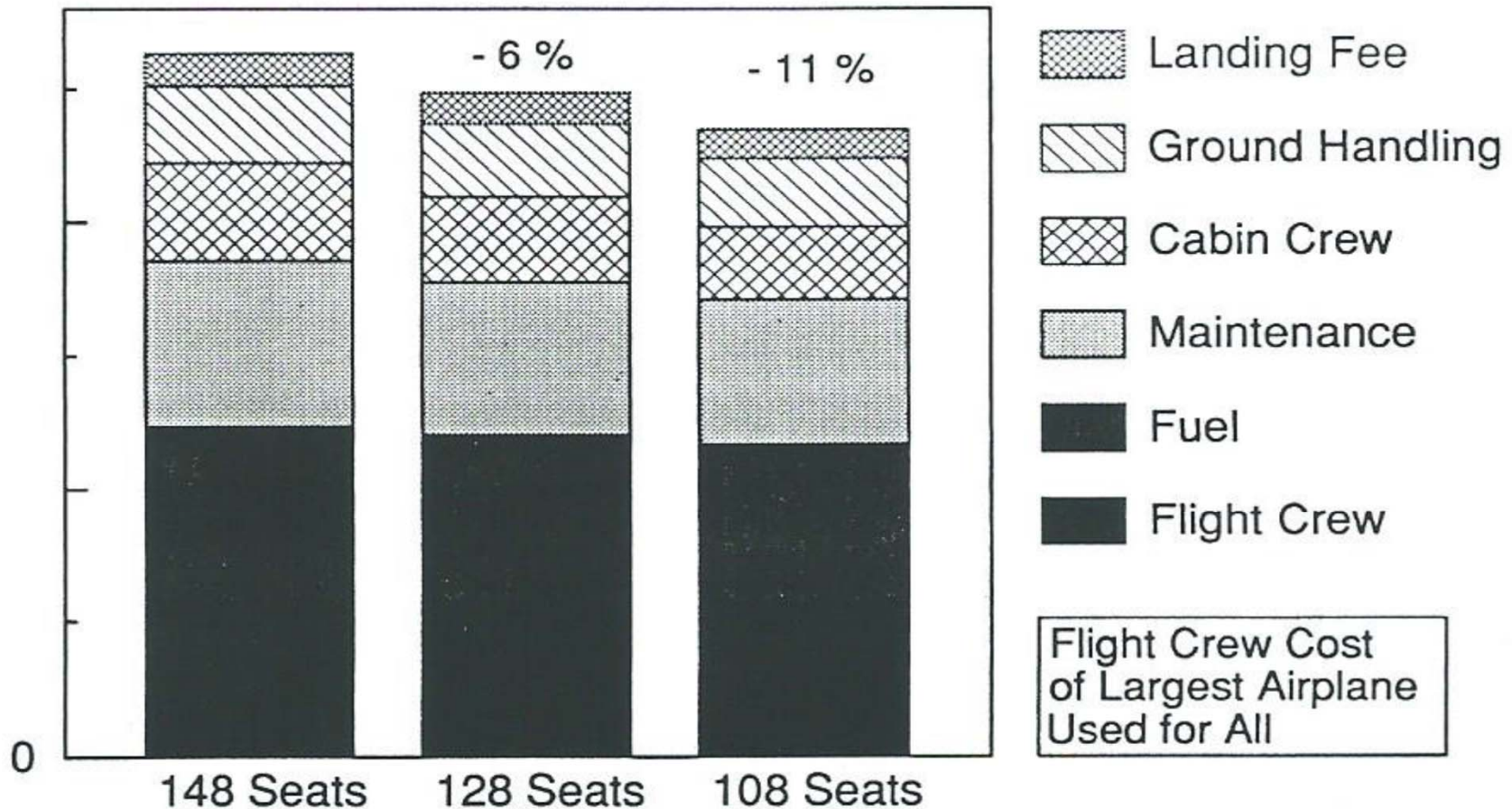
- **Adjust the capacity on flight legs during the booking process to better match actual bookings with supply by “swapping” aircraft**
- **Re-assigning available aircraft within the same fleet family**
 - Maintaining crew feasibility
 - Maintaining conservation of flow (or balance) by fleet type
 - Maintaining satisfaction of maintenance constraints
- **Also known as “Demand Driven Dispatch”**
 - Concept developed by Boeing in search of “elastic” airplane
 - Made practical by fleet commonality in aircraft families

Demand Driven Dispatch

- **Dynamic fleet assignment when demand varies daily on each flight leg during a schedule period**
 - Assign the right size airplane to each departure based on actual booking patterns
 - If bookings are forecast to be higher than average, opportunity to increase capacity for that departure
 - If bookings are forecast to be much lower than planned, reducing aircraft size can reduce total operating costs
- **Requirements for Demand Driven Dispatch (or D³)**
 - RM system that generates accurate forecasts of demand for each future flight departure date
 - Common-rated family of aircraft allows for swapping of aircraft assignments closer to departure without disturbing crew schedules

Operating Costs Differ by Aircraft Size

Airplane Operating Costs



Demand Driven Dispatch Process

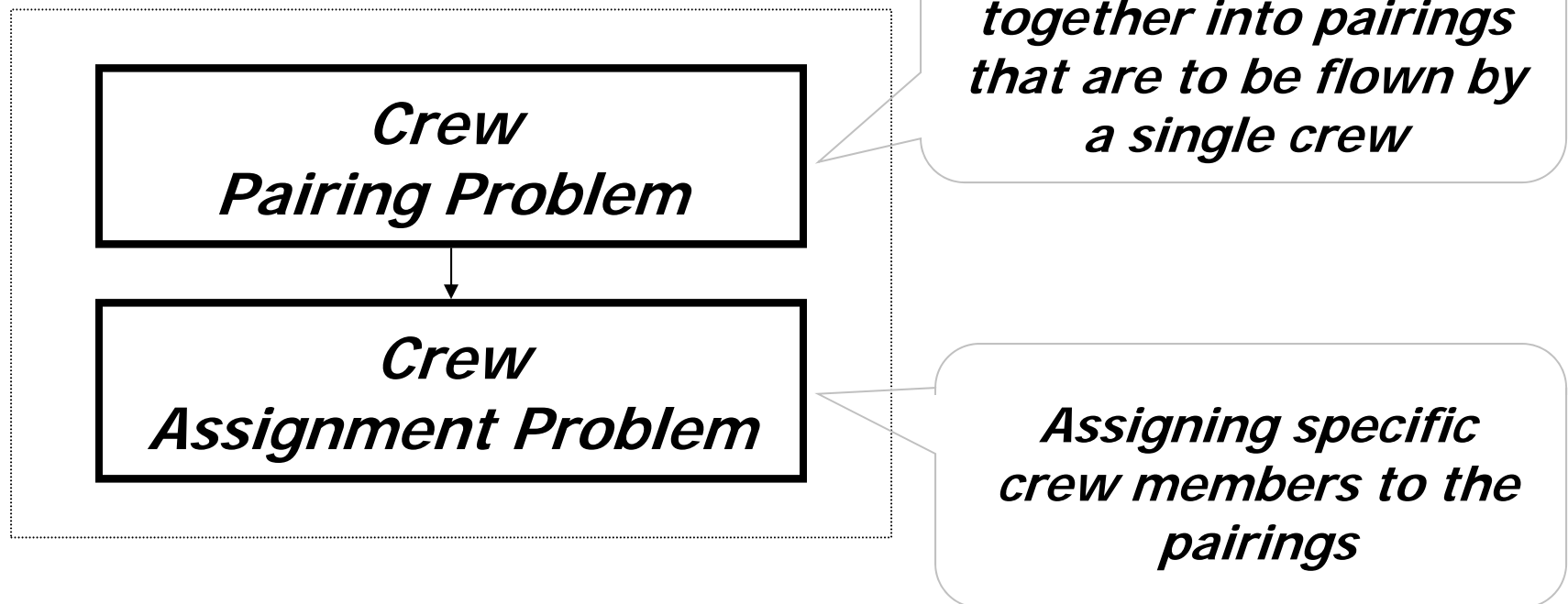
- **Identify potential swaps based on RM forecasts**
 - One flight with excess demand (greater than capacity) and another with excess capacity expected at departure
 - Both flights scheduled to depart at approximately the same time from the same airport – connecting hubs increase this potential
- **Assess benefits of executing the swap**
 - Revenue gain from assigning a larger aircraft to the flight with excess demand vs. possible spill on flight with smaller aircraft
 - Even if no revenue gains, reductions in operating costs can be achieved if both flights have excess capacity – assign smaller aircraft to the longer flight

Implementation Issues for D³

- **Crew scheduling problems can be overcome with common-rated fleet families**
 - But, larger aircraft might require additional flight attendant
- **Maintenance plans need to be maintained**
 - Swapped aircraft must return to maintenance base as scheduled
- **Ground handling and catering issues**
 - Close-in swaps tend to disrupt gate assignments and ground operations routines
- **Passenger service issues**
 - Specific aircraft type not specified until a few days before departure
 - Imposes constraints on advance seat assignment

Airline Crew Scheduling

The Crew Scheduling Problem

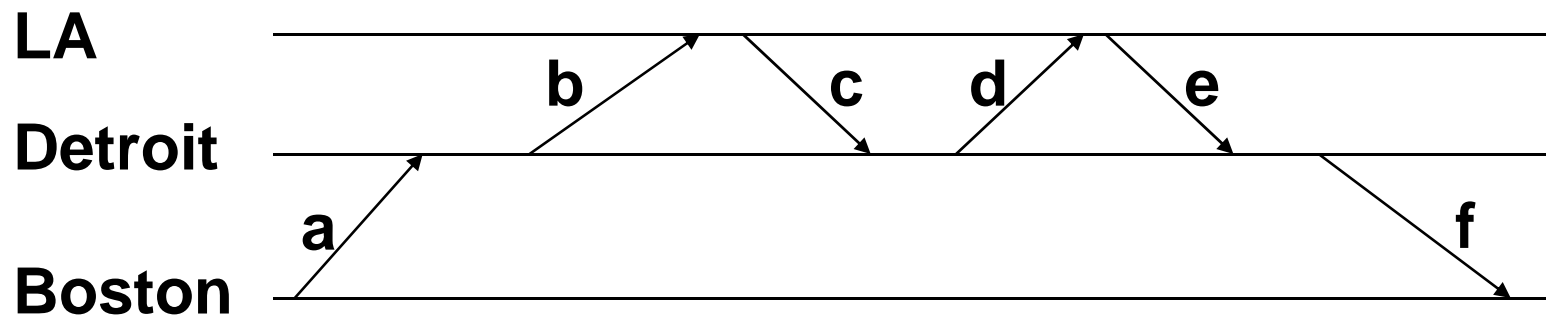


Reference: C. Barnhart, A. Cohn, E. Johnson, D. Klabjan, G. Nemhauser, and P. Vance. 2003. "Airline Crew Scheduling". Randolph W. Hall, ed. Handbook of Transportation Science, 2nd ed.

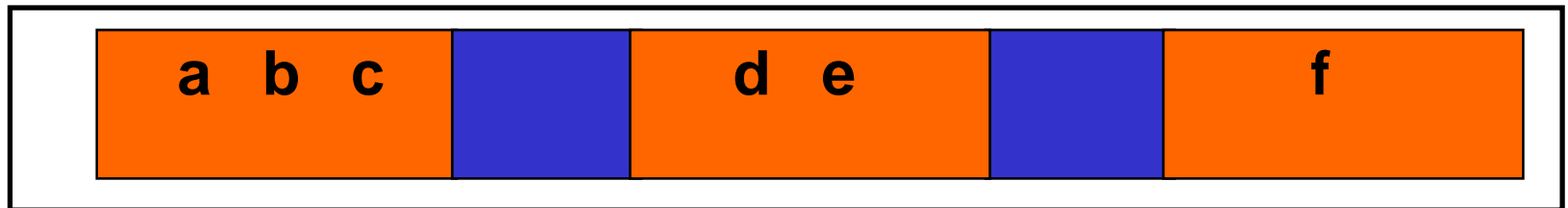
Definitions

- ***A duty period (or duty) is a sequence of flight legs comprising a day of work for a crew***
- ***A crew pairing is a sequence of duties separated by rest periods:***
 - beginning and ending at a crew base
 - spanning one or more days
 - satisfying regulations and collective bargaining agreements, such as:
 - maximum flying time in a day
 - minimum rest requirements
 - minimum connection time between two flights

Example: Duty Periods



Pairing = DP1(a,b,c) + rest + DP2(d,e) + rest + DP3(f)



Airline Crew Scheduling

- **2-stage process:**
- **Crew Pairing Optimization**
 - Construct minimum cost work schedules, called pairings, spanning several days
- **Bidline Generation/ Rostering**
 - Construct monthly work schedules from the pairings generated in the first stage
 - Bidlines
 - Individualized schedules
 - Objective to balance workload, maximize number of crew requests granted, etc.

Crew Pairing Costs

- **Duty costs: *Maximum of 3 elements:***
 - $f1$ *flying time cost
 - $f2$ *elapsed time cost
 - $f3$ *minimum guarantee
- **Pairing costs: *Maximum of 3 elements:***
 - $f1$ *duty cost
 - $f2$ *time-away-from-base
 - $f3$ *minimum guarantee

Crew Pairing Problem

- **Constraints on feasible pairings**
 - Flights connect in space and time
 - Minimum/Maximum connection times
 - Regulatory constraints
 - Maximum duty duration
 - Minimum rest duration between duties
 - 8-in-24 rule
 - Maximum time-away-from-base (TAFB)

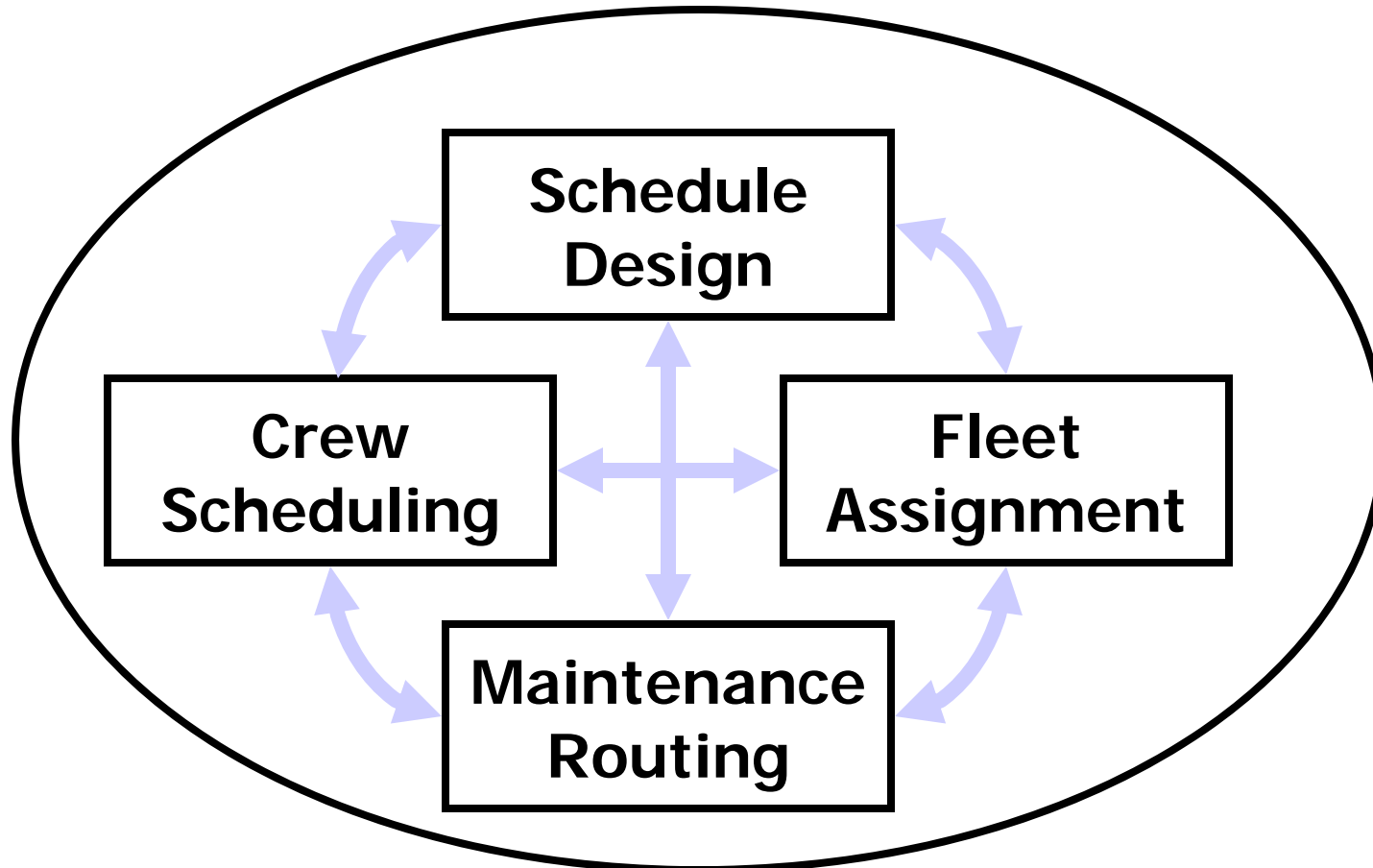
- **Potentially, many billions of pairings**

Problem Size and Solutions

- **A typical global airline (hub-and-spoke) has millions (or billions) of potential pairings**
 - 150 daily flights 90,000 pairings
 - 250 daily flights 6,000,000 pairings
- **Crews are the second highest component of aircraft operating costs (after fuel).**
- **The introduction of OR decision support tools has reduced the amount of pay & credit at some airlines by 50%.**

Integration of Schedule Optimization Models

A challenge...



SOURCE: Prof. C. Barnhart

Future Research Challenges

- 1. Integrating decisions involving schedule design and aircraft and crew routing and scheduling**
- 2. Expanding schedule planning models to include pricing and revenue management decisions**
- 3. Robust schedule planning to allow for disruptions and delays**
- 4. Operations recovery after schedule disruptions**